

Solving Rational Equations

If it is a proportion, set cross products equal.

$$\frac{7}{x-2} = \frac{11}{2x-10}$$

$$11(x-2) = 7(2x-10)$$

$$11x - 22 = 14x - 70$$

$$-22 = 3x - 70$$

$$48 = 3x$$

$$16 = x$$

- Factor all denominators.
- Find the Least Common Multiple (LCM)
- Multiply all terms by the LCM to remove all the fractions.

$$\frac{15}{x} + \frac{4}{5} = \frac{7}{x}$$

$$5x \left[\frac{15}{x} + \frac{4}{5} = \frac{7}{x} \right]$$

$$75 + 4x = 35$$

$$4x = -40$$

$$x = -10$$

LCM: $5x$

$$5x \cdot \frac{15}{x} = 75$$

$$5x \cdot \frac{4}{5} = 4x$$

$$5x \cdot \frac{7}{x} = 35$$

$$\frac{12}{x+7} = 1 - \frac{12}{x}$$

$$x(x+7) \left[\frac{12}{x+7} = 1 - \frac{12}{x} \right]$$

$$12x = x(x+7) - 12(x+7)$$

$$12x = x^2 + 7x - 12x - 84$$

$$12x = x^2 - 5x - 84$$

$$-12x \quad -12x$$

$$0 = x^2 - 17x - 84$$

$$0 = (x-21)(x+4)$$

$$x-21=0 \quad x+4=0$$

$$x=21 \quad x=-4$$

LCM: $x(x+7)$

$$x(x+7) \cdot \frac{12}{x+7} = 12x$$

$$x(x+7) \cdot \frac{12}{x} = 12(x+7)$$